

# Experimental and modeling of fixed-bed reactor for yellow phosphorous tail gas purification over impregnated activated carbon

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## Abstract

When yellow phosphorous tail gas will be used as chemical raw material gas to produce high accessional products such as formate, oxalate, methanol and so on, pretreatment process by its purifying could limit its application. In this paper, two kinds of impregnated activated carbon catalysts and catalytic oxidation reaction for purifying  $H_2S$  and  $PH_3$  contained in tail gas have been studied in laboratory-scale and pilot-plant fixed-bed reactor. The concentration of both  $H_2S$  and  $PH_3$  could be less than  $10\text{ mg/m}^3$  over these two kinds of catalysts. Reaction kinetics for the catalytic oxidation of  $H_2S$  and  $PH_3$  over the mixed catalyst has also been studied on differential reactor, and kinetic model for both compounds have been formulated, which are subsequently implemented in the modeling of the pilot-plant fixed-bed reactor. A two-dimensional un-steady reaction model which includes both physical adsorption and catalytic reaction process was developed for binary gas mixture purification in fixed-bed. Results from model calculation are reasonably well agreement with the experimental data. It is helpful for a thorough explanation of the observed pilot-plant reactor performance and designing in industrial process.

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**Keywords:** Yellow phosphorous tail gas; Catalytic oxidation; Impregnated activated carbon; Fixed bed; Modeling

## 1. Introduction

Yellow phosphorous is the main source for phosphorous chemical engineering. During the producing of yellow phosphorous by electric furnace method, about  $2500\text{--}3000\text{ m}^3$  tail gas will be let out when 1 t yellow phosphorous was produced, which is one of the main sources for air pollution in most cities in PR China [1]. The main contain of yellow phosphorous tail gas is about 85–95% carbon monoxide, which cause damage for environment and a huge waste of CO when it is exhaust into atmosphere. Since 1980's,  $C_1$  chemistry had got a great development especially in CO synthesizing technology. Many products such as methylformiate, dimethylether, ethanoic acid, methanol and methyl carbonate can be synthesized from CO. If yellow phosphorous tail gas can be used as raw material gas to synthesize chemically product, it cannot only avoid environmental pollution but also reduce the cost of yellow phosphorous production. However, by now only 20–25% yellow phosphorous tail gas has been used as fuel and the rest is let out into

the air, few of them is used to produce some cheap products such as trimeric sodium phosphate, etc. [2]. The main reason to restrict wildly use of yellow phosphorous tail gas is that it contains phosphorous ( $PH_3$ ,  $P_4$ ), sulfur ( $H_2S$ ), which can stark influence the reaction of carbonyl combination even at very low concentration. The heat value of tail gas is about  $10,000\text{ kJ/m}^3$ . How to multipurpose use yellow phosphorous tail gas is one of the valuable things. It must obtain high purity CO when it is used as chemical raw material. Therefore, yellow phosphorous tail gas must be pretreated before it is used.

For the purposes of further products of yellow phosphorous tail gas, purifying technology have been researched for many years such as: washing with water to get rid of fly ash,  $SiF_4$  and part of  $H_2S$  and HF; washing with water and sodium (NaOH 10–15%); purifying with the method of TSA-PSA [3,4], etc. For some high quality required of CO, deep desulfurization and dephosphorous (both sulfur and phosphorous contained less than 1 ppm) technologies are needed.

During the past several decades, most researches were focus on removing  $H_2S$  by adsorption and catalytic oxidation methods. Westmoreland and Harrison [5] researched that some metal oxide such as Fe, Zn, Mo, Mn, Sr, B, Co, Cu and W have better capacity for  $H_2S$  removal. Many works were focus on  $H_2S$

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### Nomenclature

$b_i$	Langmuir constant of $i$
$c_i$	$i$ concentration in gas phase (kg/m <sup>3</sup> )
$c_i^*$	$i$ concentration at equilibrium (kg/m <sup>3</sup> )
$d$	diameter of fixed bed (m)
$D_{zi}$	axial diffusion constant of $i$
$D_{ri}$	radius diffusion constant of $i$
$k$	reaction rate constant of PH <sub>3</sub> (1/min)
$k_1$	reaction rate constant of H <sub>2</sub> S (kg/s Pa)
$k_2$	reaction rate constant of H <sub>2</sub> S (1/Pa)
$K$	adsorption mass transfer constant (m <sup>3</sup> /kg s)
$Q_{mi}$	monolayer maximum adsorption amount (kg/kg)
$r$	radius of fixed bed (m)
$R_i$	reaction rate of $i$ (kg/s m <sup>3</sup> )
$S_{cat}$	catalytic surface area per unit catalyst volume (m <sup>2</sup> /m <sup>3</sup> )
$t$	time (s)
$u$	flow velocity (m/s)
$W_S$	amount of S loading on catalyst (kg/kg)
$X_i$	$i$ loading in activated carbon (kg/kg)
$z$	length of fixed bed (m)

### Greek letters

$\varepsilon$	voidage of fixed bed
$\rho_c$	density of activated carbon (kg/m <sup>3</sup> )

### Superscript

*	at equilibrium
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### Subscript

$i$	compound index of gas
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removal from coal gas by limestone adsorbents [6–10]. However, less report had been found about PH<sub>3</sub> removal from gas phase except chemical vapor deposition [11,12]. Among various methods for H<sub>2</sub>S and PH<sub>3</sub> removal reported in the literature, catalytic oxidation at low temperature is less reported [13–16]. To our knowledge, there is no systematic study of binary mixture gas purification contained both H<sub>2</sub>S and PH<sub>3</sub> at very low concentration, and this is the sticking point for yellow phosphorous tail gas purification.

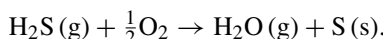
In the previously work of our group, it has been found that activated carbon impregnated with metal and other solution has better adsorption capacity for sulfur and phosphorous removing from tail gas. During this process, catalytic oxidation reaction for H<sub>2</sub>S and PH<sub>3</sub> take place over impregnated activated carbon. Therefore, it can be assumed that physical adsorption and catalytic oxidation reaction occur simultaneously. In the present work, adsorption isotherm, dynamic behavior and chemical kinetics have been studied over impregnated activated carbon for desulfurization and dephosphorous. The influences of operating variables on catalytic oxidation in both laboratory-scale and pilot-plant fixed bed were investigated. For the purpose of optimal designing of gas–solid reactor and seeking for the optimal operation condition, a simulation model also has been given for

predicting the process of both physics adsorption and chemical reaction for mixture gas in fixed-bed reactor.

## 2. Mechanism

The mechanism of removing H<sub>2</sub>S has been studied including adsorption-adsorption process, liquid redox process and direct oxidation at lower temperature in presence of a catalyst [17,18]. Highly removal efficient and high sulfur capacity up to 60% (g/g cat.) are obtained by catalytic oxidation over impregnated activated carbon [19]. Whereas less study has been found about the removal of PH<sub>3</sub> from mixed gases.

The prior investigation for catalytic reaction on activated carbon was



Elemental sulfur formed in the oxidation is deposited on carbon catalyst which causes the continuous change in effectiveness factor due to the texture of catalyst changing as a result of sulfur deposition and gradual decrease in the number of active sites due to their physical covering by sulfur [20]. The amount of sulfur formed on is plotted against the reciprocal of time to processing the data. For removal of H<sub>2</sub>S in yellow phosphorous tail gas over impregnated activated carbon, catalytic oxidation reaction takes place at the existing of O<sub>2</sub>. At the same time, reactions may take place simultaneously for P<sub>4</sub> and PH<sub>3</sub> existed in tail gas, which will be analyzed below.

An ample amount of O<sub>2</sub> contained in tail gas could be used in these catalyst oxidation reactions. Previous work in our group had shown that in addition to oxidation-reductive reaction of impregnated activated carbon bed, there were some H<sub>2</sub>S and PH<sub>3</sub> reduction in tail gas through the carbon bed at different temperature. Therefore, it can be assumed that physical adsorption and catalytic oxidation reaction occur simultaneously over the impregnated activated carbon.

### 2.1. Equilibrium adsorption of gas mixture

Except H<sub>2</sub>S and PH<sub>3</sub>, yellow phosphorous tail gas contains about 85–90% CO, 2–5% N<sub>2</sub>, 1–8% H<sub>2</sub>O, 1–4% CO<sub>2</sub>, 0.5% H<sub>2</sub> and 0.3% CH<sub>4</sub> and 0.5% O<sub>2</sub>. The measurement of mix-gas adsorption is certainly tedious. However, models or correlation for mixed-gas adsorption should be capable of predicting from pure gas isotherms. Langmuir isotherm for single-gas adsorption can readily be extended to an  $n$ -component mixture [21]. The Langmuir equation for single component is:

$$X = \frac{Q_m b y}{1 + b y} \quad (1)$$

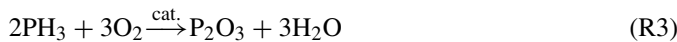
When adsorption for a mixture gas, supposing each species maintains its own molecular area, and the area covered by one molecule that is not influenced by the presence of other species on the surface as in single-gas adsorption, the amount adsorbed for  $i$  in the mixture is:

$$X_i = \frac{Q_{mi} b_i c_i}{1 + \sum_i^n b_i c_i} \quad (2)$$

For the adsorption of tail gas, taking H<sub>2</sub>S and PH<sub>3</sub> as an representation for sulfur and phosphorous components and only these two components are adsorbed on carbon, the rest compounds in tail gas were considered as an inert gas which cannot be adsorbed on adsorbent, therefore Eq. (2) would be calculated for binary mixture gas for H<sub>2</sub>S and PH<sub>3</sub> ( $n=2$ ).

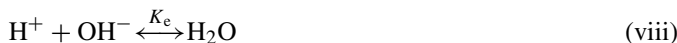
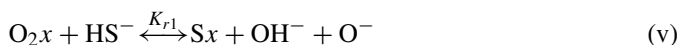
## 2.2. Chemical reaction kinetic of H<sub>2</sub>S and PH<sub>3</sub>

During the physical adsorption process for H<sub>2</sub>S and PH<sub>3</sub>, catalytic oxidation reaction take place under the existing of oxygen contained in tail gas over impregnated activated carbon. The mechanisms associated with oxidation process are summarized as follow:



P<sub>4</sub> and PH<sub>3</sub> were oxide into P<sub>2</sub>O<sub>3</sub> and P<sub>2</sub>O<sub>5</sub> in fixed bed. The adsorptive capacity for P<sub>2</sub>O<sub>3</sub> and P<sub>2</sub>O<sub>5</sub> is far more than that for P<sub>4</sub> and PH<sub>3</sub>, therefore P<sub>2</sub>O<sub>3</sub> and P<sub>2</sub>O<sub>5</sub> were adsorbed on the impregnated activated carbon. S was adsorbed on the impregnated activated carbon finally as a oxidation product of H<sub>2</sub>S, here the impregnated activated carbon take the role of adsorbent and catalyst. Catalyst out of service can be regenerated.

Kinetic mechanism for H<sub>2</sub>S oxidation can be summarized as four steps: diffusion–dissolution–adsorption–reaction. When tail gas goes into the reactor, part of aqueous contained in the gas was adsorbed on activated carbon and became a thin membrane. H<sub>2</sub>S and O<sub>2</sub> molecules diffused into the pore of solid particle and solved in the aqueous membrane and then deposited. This mechanism, listed below, consists of eight independent forward pathways for oxidation of H<sub>2</sub>S, and their corresponding kinetic rate expressions.



Step (v) was supposed as a control process and step (vi) and (vii) was transient reaction, the solved of H<sub>2</sub>S and O<sub>2</sub> fits Henry

law in (i) and (ii), the rate of reaction for H<sub>2</sub>S are of the form:

$$r_s = -r_A = K_{r1}C_{O_2x}C_{HS^-} + K_{r2}C_{ox}C_{HS^-} = 2K_{r1}C_{O_2x}C_{HS^-} \quad (\text{3})$$

$$r_A = \frac{2K_{r1}K_{e1}C_{xt}K_{HB}K_aP_{O_2}P_{H_2S}}{[H^+](1 + K_aK_{HB}P_{O_2})} \times \phi_S \quad (\text{4})$$

where  $\phi_S = 1 - C_{sx}/C_{xt}$  is the function of S deposition.

Reaction rate can be express using the rate of S deposited in per gram catalyst as follow:

$$r_A = \frac{1}{M_S} \frac{dW_S}{dt} = \frac{2K_wK_{r1}C_{xt}K_{e1}K_{HA}K_{HB}K_aP_{O_2}P_{H_2S}}{[H^+](1 + K_aK_{HB}P_{O_2})} \times \phi_S \quad (\text{5})$$

where  $K_w$  is the kinetic rate constant which is dependent on the frame of catalyst (impregnated activated carbon) and contents of H<sub>2</sub>O in gas,  $W_S$  the adsorbed amount of S per gram adsorbent,  $M_S$  the molar quality of S,  $\phi_S$  the function of  $W_S$  and saturation S deposited, used a empirical function to replace Eq. (5)

$$\phi_S = (1 - aW_S)^n \quad (\text{6})$$

therefore reaction rate can be expressed as:

$$\frac{dW_S}{dt} = \frac{2M_SK_wK_{r1}(k'/a)K_{e1}K_{HA}K_{HB}K_aP_{O_2}P_{H_2S}}{[H^+](1 + K_aK_{HB}P_{O_2})} \times (1 - aW_S)^n \quad (\text{7})$$

or:

$$\frac{dW_S}{dt} = \frac{(k_1k_2/a)P_{O_2}P_{H_2S}}{(1 + K_2P_{O_2})} \times (1 - aW_S)^n \quad (\text{8})$$

$$k_1 = \frac{2M_SK_wK_{r1}K_{e1}K_{HA}}{[H^+]} \quad (\text{9})$$

$$k_2 = K_aK_{HB} \quad (\text{10})$$

where  $a = k'/C_{xt}$ .

For catalytic oxidation reaction of phosphorous, PH<sub>3</sub> was taken as a representation (which is the main container of total phosphorous in tail gas). The reaction process for PH<sub>3</sub> catalytic oxidation reaction (such as R4) may consist of three steps: diffusion from bank of gas to the surface of catalyze (external diffusion), diffusing from surface to the internal surface of catalyze (internal diffusion), PH<sub>3</sub> was adsorbed on the internal surface of catalyze and oxidation reaction took place. The products of oxidation reaction was adsorbed on the surface of catalyze such that the activated center site of catalyze was reduced and finally got saturation. The reaction rate can be expressed:

$$r = -\frac{dC_A}{dt} = \frac{dC_P}{dt} = k_{CA}^n \quad (\text{11})$$

where  $C_A$  represents the concentration of reaction A,  $C_P$  the concentration of products,  $t$  the reaction time,  $k$  means the reaction constant and  $n$  is the reaction order.

### 2.3. Fixed-bed mathematical model of binary gas adsorptive reactor for isothermal dilute systems

According to the analysis above, the mechanism of removing H<sub>2</sub>S and PH<sub>3</sub> from yellow phosphorous tail gas over activated carbon impregnated is that catalytic oxidation reaction and physical adsorption took place simultaneously. From an engineering point of view, solving the complete equations of mass, momentum and heat transfer equations requires large computational effort [22,23]. During the past decades, many methods have been employed to model adsorption processes including physical and chemical adsorption in fixed bed [24–29]. Huang et al. [30] proposed a model for gas–solid chemisorption in chemical heat pumps, Wang et al. [31] had studied H<sub>2</sub>S catalytic oxidation on impregnated activated. In this work, a new adsorptive reactor model including physical adsorption and chemical reaction occurred simultaneously will be presented to describe the binary gases dynamic behavior for H<sub>2</sub>S and PH<sub>3</sub> removing from yellow phosphorous tail gas in fixed bed.

In the case of diluted systems, adsorbed amount of compounds is very small comparing with the total amount of gases entering the column, it is reasonable to suppose that gas density is constant over the entire bed. For this reason, momentum equation can be simplified to obtain a constant profile of velocity not depending on the axial direction. By assuming a quasi-steady, incompressible flow, the two-dimensional mass balance equation for fixed-bed reactor take the form as below:

$$\varepsilon \frac{\partial c_i}{\partial t} = \frac{\partial}{\partial z} \left( D_{zi} \frac{\partial c_i}{\partial z} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left( r D_{ri} \frac{\partial c_i}{\partial r} \right) - u \frac{\partial c_i}{\partial z} - (1 - \varepsilon) \rho_c \frac{\partial X_i}{\partial t} - (1 - \varepsilon) S_{\text{cat}} R_i \quad (12)$$

where  $\varepsilon$  is bed voidage,  $D_{zi}$  is mass diffusivity for gas species  $i$  of axial,  $D_{ri}$  means mass diffusivity for gas species  $i$  of radial, which could be calculated through the method of ref. [32].  $c_i$  is  $i$  component concentration in gas,  $X_i$  the adsorbed amount  $i$  on solid surface,  $\rho_c$  the density of solid,  $S_{\text{cat}}$  the catalytic surface area per unit catalyst volume and  $R_i$  is the reaction rate of  $i$ .

The boundary conditions for radius are given below:

$$r = \frac{d}{2}, \quad \frac{\partial c_i}{\partial r} = 0 \quad (13)$$

$$r = 0, \quad \frac{\partial c_i}{\partial r} = 0 \quad (14)$$

also condition to axial coordinate are:

$$z = 0, \quad u(c_{\text{ai}} - c_i) = -D_{zi} \frac{\partial c_i}{\partial z} \quad (15)$$

$$z = L, \quad \frac{\partial c_i}{\partial z} = 0 \quad (16)$$

the initial condition for mass balance equation is:

$$t = 0, \quad \begin{cases} c_i(0, r, z) = c_{i0} \\ X_i(0, r, z) = X_{i0} \end{cases} \quad 0 \leq r \leq \frac{D}{2}, \quad 0 \leq z \leq L \quad (17)$$

adsorption mass transfer rate can be written as:

$$\frac{\partial X_i}{\partial t} = K(c_i - c_i^*) \quad (18)$$

where  $c_i^*$  is the adsorption equilibrium concentration for  $i$  in gas phase calculated by Eq. (2).

## 3. Experiment and set up

### 3.1. Impregnated activated carbon preparation

Two kinds of impregnated activated carbon were prepared. Activated carbon (volume density is 0.67 g/cm<sup>3</sup>, BET surface area is 1150 m<sup>2</sup>/g, particle size used in experiment is about 2 mm) bought from company was used as the support. Firstly, activated carbon was washed and dried at 100–110 °C for 24 h. For one impregnated activated carbon (named JAC), a known amount of dried activated carbon was stirred in 7% NaCO<sub>3</sub> aqueous solution at room temperature for 12 h, and then dried at 110 °C for another 24 h. For another one (named SAC), a known amount of dried activated carbon was impregnated in 5% HCl aqueous solution for 36 h, and then dried at 110 °C for more than 14 h. Before the adsorption experiment, catalysts were activated in situ in a quartz vial adsorber under ultra-pure N<sub>2</sub> at 120 °C at 1 °C/min and the temperature held at that point for 10 h.

### 3.2. Experimental apparatus and chemical reaction dynamics measurements

#### 3.2.1. Laboratory-scale fixed-bed reactor

An U form quartz adsorber with 10 mm i.d. was employed. Nitrogen (pre-purified grade, Metro welding, 99.995%) was used as the carrier gas and by blending with amount of O<sub>2</sub> and pure H<sub>2</sub>S or PH<sub>3</sub>, the mixture gas was directed into the adsorber. Analysis of reactor inlet and outlet gas was carried out by a FID spectrometer and a gas chromatography (type 120G). Experimental tail gas was absorbed using Na<sub>2</sub>CO<sub>3</sub> and Cu<sub>2</sub>SO<sub>4</sub> solution, respectively.

#### 3.2.2. Pilot-plant reactor

A pilot-plant scale experiments of catalytic oxidation were performed in a fixed-bed column with the internal diameter of 0.24 m, height of 2.8 m and gas volume of 50 N m<sup>3</sup>/h. The fixed-bed column and yellow phosphorous tail gas were heated by steam indirectly. A schematic flow diagram of catalytic oxidation process is shown in Fig. 1 Experiments were carried out at different temperatures within the range of 20–90 °C. Analysis of the reactor in- and outlet gas was carried out by a FID spectrometer and a gas chromatography (type 120G). The contents of component of yellow phosphorous tail gas used in this experiment described in Table 1.

#### 3.2.3. Chemical kinetics

Chemical kinetics experiment had been studies in a differential reactor with 10 mm i.d. and 500 mm in length stainless steel tube. The concentration of H<sub>2</sub>S or PH<sub>3</sub> in mixture gas was regulated by carrier gas (N<sub>2</sub> and amount of O<sub>2</sub>) and pre-heated before

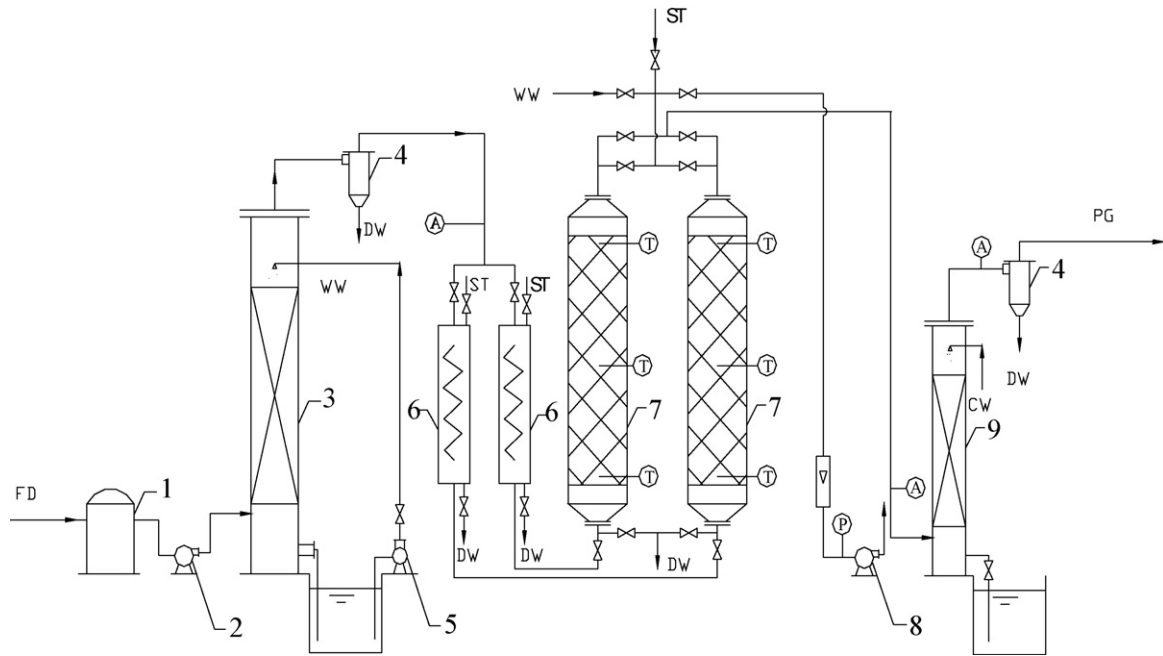


Fig. 1. Flow sheme of the apparatus for phosphorous tail gas purification: (1) water seal, (2) vacuum pump, (3) caustic washing tower, (4) mist eliminator, (5) pump, (6) preheated, (7) reactor, (8) induced fan, (9) cooler. T, thermometer; P, pressure gauge; A, sampling.

enter the reactor. Both  $H_2S$  and  $PH_3$  flow rates were adjusted by mass-flow meters, respectively. For a reactor being differential is that the conversion of reactants in the bed is extremely small as the change in reactant concentration through the bed. That means, the reactor is considered to be gradient-less, and reaction rate is considered spatially uniform with the bed. Reaction rate is calculated as follow:

$$(-r_A) = \frac{G}{V_R}(C_{Af} - C_{Ao}) \quad (19)$$

where  $-r_A$  is the reaction rate for reactant concentration is  $C_{Af} + C_{Ao}/2$ . In each experiment, 1.0 g catalysts with particle size  $1.0 \mu m$  were in use.  $G$  is the volume rate of reactant.

For  $H_2S$  removal, from Eq. (8), the rate of S depositing can be expressed by:

$$\frac{dW_S}{dt} = r_{S0} \times (1 - aW_S)^n \quad (20)$$

where  $r_{S0}$  represents the initial rate at  $W_S = 0$ :

$$r_{S0} = \frac{k_1 k_2 / a P_{O_2} P_{H_2S}}{(1 + K_2 P_{O_2})} \quad (21)$$

the deposit amount of S is calculated from Eq. (20)

$$W_S = \left\{ \begin{array}{l} \frac{[1 - \exp(-ars_0 t)]}{a} (n = 1) \\ \frac{1}{a} \left\{ 1 - \frac{1}{[1 + (n-1)ars_0 t]^{1/n-1}} \right\} (n \neq 1) \end{array} \right\} \quad (22)$$

where  $n$ ,  $a$  and  $r_{S0}$  can be simulated through experiments. When  $n=2$ , the calculation results shows the best relatively, therefore, for  $n=2$ , the Eq. (22) will be:

$$\frac{1}{W_S} = a + \frac{1}{r_{S0} t} \quad (23)$$

$a$  and  $r_{S0}$  can be calculated from the slop and intercept of line  $1/W_S \sim 1/t$ . Results of  $a$  at different temperature are listed in Table 2. The relationship between  $a$  and temperature is fitted with line can be expressed by:

$$a = -1.3219 + 0.1217(T_T - 273.1) \quad (24)$$

Kinetic constants  $k_1$  and  $k_2$  in Eq. (8) could be got through Arrhenous equation at different temperature and expressed as

Table 1  
Contents of component in yellow phosphorous tail gas

Component	Content (%)	Component	Content
CO <sub>2</sub>	2.44	N <sub>2</sub>	4.29%
O <sub>2</sub>	0.5	H <sub>2</sub> O	~5%
CO	85.425	H <sub>2</sub> S	1050 mg/m <sup>3</sup>
H <sub>2</sub>	6.47	P <sup>a</sup>	1170 mg/m <sup>3</sup>
CH <sub>4</sub>	0.425	HF	310 mg/m <sup>3</sup>

<sup>a</sup> The total phosphorous containing in the tail gas.

Table 2  
Kinetic parameter at different temperature

	$T$ (°C)				
	20	45	60	75	90
$a^a$	1.548	3.635	5.734	7.842	9.938
$k$ (1/min $\times 10^{-3b}$ )	3.093	1.508		0.789	0.396

<sup>a</sup> Calculated from Eq. (23).

<sup>b</sup> Kinetic constant for  $PH_3$  come from the slope of lines in Fig. 2.



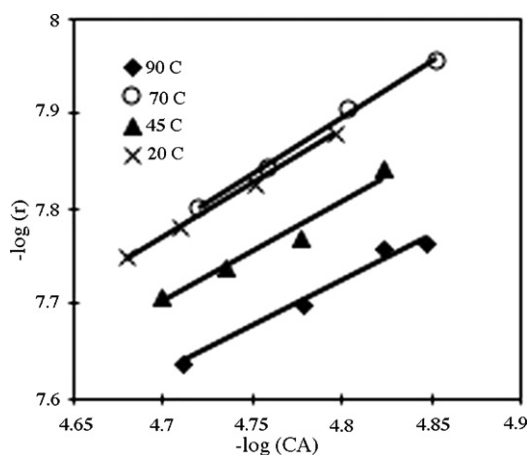


Fig. 2. The relationship between  $\log r \sim \log C_A$  at different temperature.

follows:

$$k_1 = 2.271 \times 10^5 \exp \left[ \frac{-2698.8}{T_r} \right] \quad (25)$$

$$k_2 = 0.108 \exp \left[ \frac{2192}{T_r} \right] \quad (26)$$

For  $\text{PH}_3$ , from Fig. 2 it can be seen that it was a line relationship between  $\log r \sim \log C_A$ , that means the reaction order  $n=1$ , and kinetic constant can be calculated through the slope and intercept of line  $\log r \sim \log C_A$ . Results are also listed in Table 2.

#### 4. Numerical solutions

A system of Eq. (12) accompanied by four boundaries (Eqs. (13)–(16)) and one initial condition (Eq. (17)) for two compounds ( $\text{H}_2\text{S}$  and  $\text{PH}_3$ ) are solved simultaneously by finite-difference method. Space grid is chosen to be 0.004 m in radial ( $\Delta r$ ) and 0.07 m in axial ( $\Delta z$ ), and corresponding time step-size ( $\Delta t$ ) being 10 s. Mass transfer process within  $\Delta v$  ( $\Delta v = \Delta r \times \Delta z$ ) during  $\Delta t$  were supposed to be steady. At the same time, the affection of fluid flow distribution in radial were also in computing. The parameters used in calculating were listed in Table 3.

#### 5. Results and discussion

Two impregnated activated carbon, SAC and JAC, were firstly tested in laboratory-scale fixed-bed adsorber at 20 °C. The breakthrough curves of  $\text{H}_2\text{S}$  and  $\text{PH}_3$  adsorption on these two kinds of adsorbents are shown in Figs. 3 and 4. It is indicated that the adsorption capacity of SAC was higher for  $\text{PH}_3$  than for  $\text{H}_2\text{S}$ , whereas the adsorption capacity of JAC was better for  $\text{H}_2\text{S}$  than for  $\text{PH}_3$ . Breakthrough time is 2000 min for  $\text{H}_2\text{S}$  JAC and 500 min for  $\text{PH}_3$  on SAC. When adsorbents were used oppositely,  $\text{H}_2\text{S}$  was adsorbed on SAC and  $\text{PH}_3$  was adsorbed on JAC, breakthrough time is only approximately 10 min for both two adsorbates. It is clear that there will not get desirous results for purification real yellow phosphorous tail gas only using one

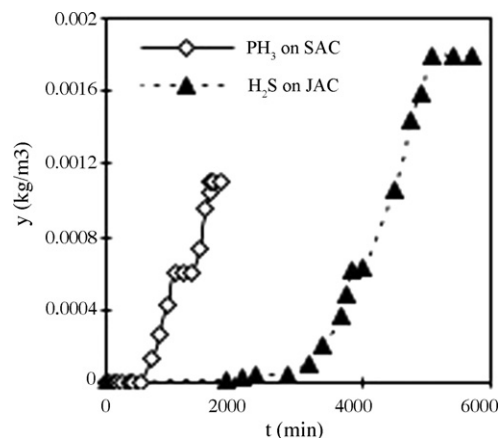


Fig. 3. Breakthrough curve of  $\text{H}_2\text{S}$  adsorption on JAC and  $\text{PH}_3$  adsorption on SAC.

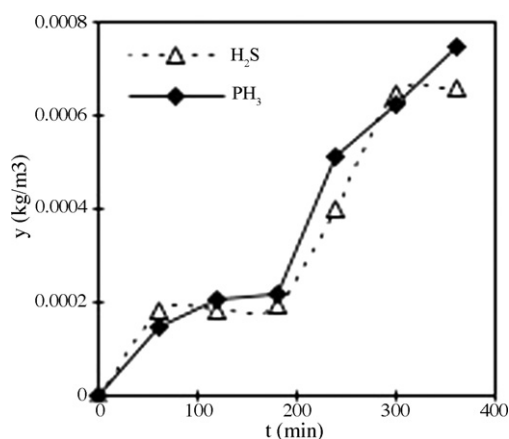


Fig. 4. Breakthrough curve of  $\text{H}_2\text{S}$  adsorption on SAC and  $\text{PH}_3$  adsorption on JAC.

of these impregnated activated carbon as an adsorbent. Fig. 5 shows the breakthrough curves for  $\text{H}_2\text{S}$  and  $\text{PH}_3$  on a mixture adsorbent (half of SAC and half of JAC) at room temperature. It is clear that the mixture adsorbent has better adsorption capacity for both  $\text{H}_2\text{S}$  and  $\text{PH}_3$ , although the adsorption capacity for these two compounds are less than that one adsorbent for pure component shown in Fig. 3, it will be useful for P and S

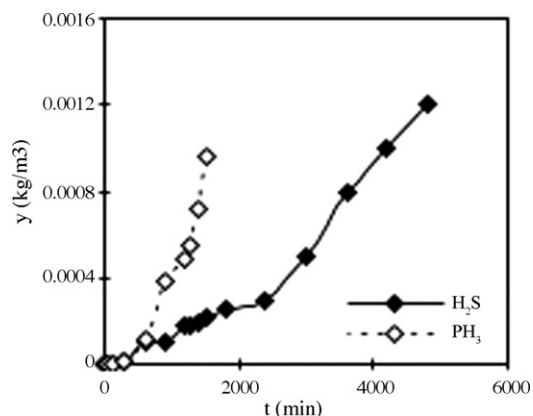


Fig. 5. Breakthrough curve of  $\text{H}_2\text{S}$  and  $\text{PH}_3$  adsorption on mixture sorbent at 20 °C.

Table 3  
Simulation parameters for isotherms and model calculation

$\varepsilon$	$\rho_c$ (kg/m <sup>3</sup> )	$K$ (m <sup>3</sup> kg s <sup>-1</sup> )	$z$ (m)	$\Delta z$ (m)	$d$ (m)	$\Delta r$ (m)	$X_0$ (kg kg <sup>-1</sup> )	$\Delta t$ (s)
0.37	670	0.028	2.8	0.07	0.24	0.004	$1 \times 10^{-8}$	10
				$Q_m$	$b$			
H <sub>2</sub> S				0.2789	665.84			
PH <sub>3</sub>				0.00134	1636.31			

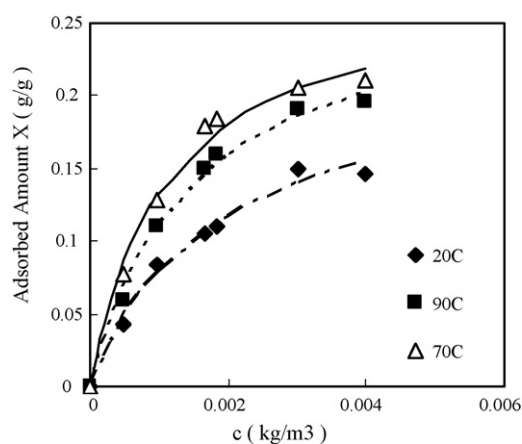


Fig. 6. Adsorption isotherms of H<sub>2</sub>S on impregnated activated carbon, at different temperature, solid or dash line is fitted with Langmuir model.

removal simultaneously for real yellow phosphorous tail gas in industry.

The first step in the characterization of a material for a specific adsorption separation process is to measure the adsorption equilibrium of pure components. Adsorption equilibrium of pure H<sub>2</sub>S and PH<sub>3</sub> at different temperature are shown in Figs. 6 and 7. Langmuir isotherm model was used to fit and analyze the data of pure gases used in this work. Fitted parameters used in Eq. (2) are listed in Table 3. It is noticed that the adsorbent has better adsorption capacity for both H<sub>2</sub>S and PH<sub>3</sub> at 70 °C. Therefore, reaction temperature at pilot-scale was taken at 70 °C.

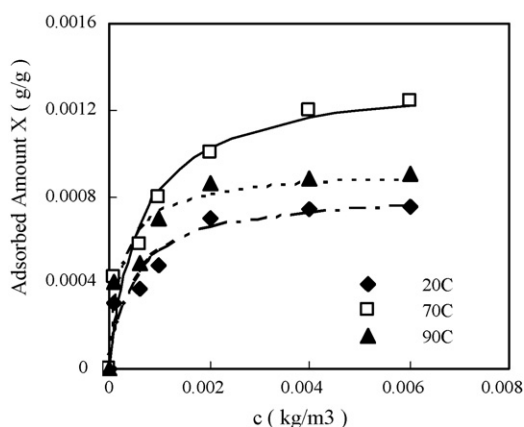


Fig. 7. Adsorption isotherms of PH<sub>3</sub> on impregnated activated carbon, at different temperature, solid or dash line is fitted with Langmuir model.

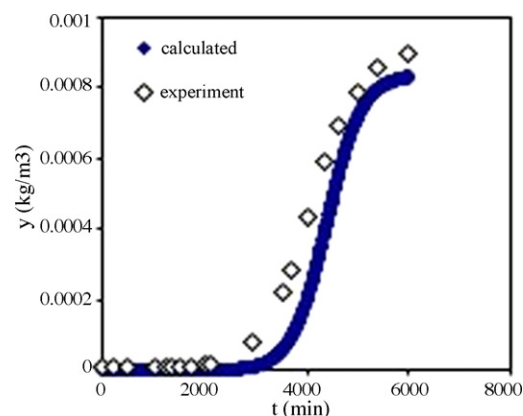


Fig. 8. Comparing breakthrough curve of experiment in pilot-plant scale reactor using model gas (N<sub>2</sub> and amount of O<sub>2</sub>) with model predicted for H<sub>2</sub>S adsorption at 70 °C, space velocity 800 h<sup>-1</sup>.

Fig. 8 compares the breakthrough curve between calculation by modeling and measured data in pilot-plant scale reactor using model gas (N<sub>2</sub> and amount of O<sub>2</sub>) for H<sub>2</sub>S removal. Model prediction is good agreement with experimental.

Fig. 9 shows the breakthrough curve of PH<sub>3</sub> come from model predicting and experiment in pilot-plant reactor for real yellow phosphorous tail gas. Model predicting is agreement with experiment. The error between predicted and experiment may contribute from the affect of other low concentration compounds contained in tail gas listed in Table 1. At this time, H<sub>2</sub>S in the out-

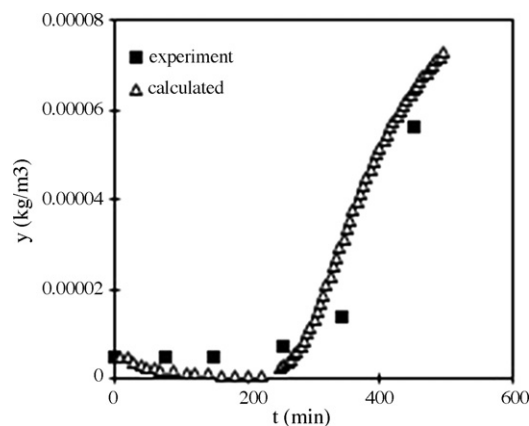


Fig. 9. Comparing breakthrough curve of experiment in pilot-plant reactor for real yellow phosphorous tail gas with model predicted for PH<sub>3</sub> adsorption at 70 °C, space velocity 400 h<sup>-1</sup>.

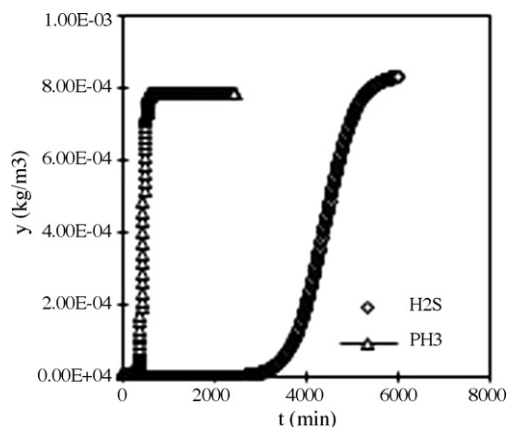


Fig. 10. Comparing breakthrough curve of H<sub>2</sub>S and PH<sub>3</sub> on pilot-plant reactor by model prediction at 70 °C 800 h<sup>-1</sup>.

let of reactor cannot be tested, that means during the pilot-plant process reaction time is mainly depended on the breakthrough time of PH<sub>3</sub>.

Fig. 10 shows the outlet concentration varieties with time for H<sub>2</sub>S and PH<sub>3</sub> by model calculated in pilot-plant reactor. Comparing with Fig. 5, it is indicated that due to the catalytic oxidation reaction taking place breakthrough time difference between H<sub>2</sub>S and PH<sub>3</sub> increased, which means at this reaction condition the selective of catalyze is more higher for H<sub>2</sub>S than for PH<sub>3</sub>. Breakthrough time of H<sub>2</sub>S is nearly 3000 min at 800 h<sup>-1</sup> space velocity, it is almost 10 times than that of PH<sub>3</sub>. Figs. 8 and 9 also indicated the same results.

Figs. 11 and 12 show the concentration distribution of H<sub>2</sub>S and PH<sub>3</sub> in gas phase in the reactor alone radial and axial at 300 min and 600 h<sup>-1</sup> space velocity by model prediction. It is clear that the concentration of both gas compounds decreased from centre to the wall in the radius. Figs. 13 and 14 show the concentration distribution in the middle of reactor in axial at different time by model calculation. From the model prediction, it is easy to know the detail concentration distribution of component in reactor. It is useful for designing of a real yellow phosphorous tail gas purification plant.

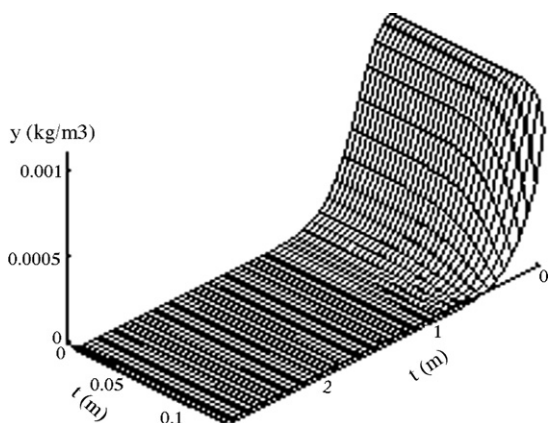


Fig. 11. Concentration distribution of H<sub>2</sub>S in gas phase in the reactor alone radial and axial at 300 min and 600 h<sup>-1</sup> space velocity by the model prediction.

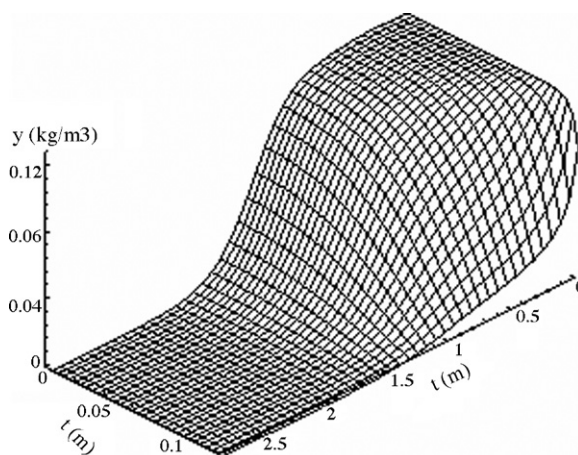


Fig. 12. Concentration distribution of PH<sub>3</sub> in gas phase in the reactor alone radial and axial at 300 min and 600 h<sup>-1</sup> space velocity by the model prediction.

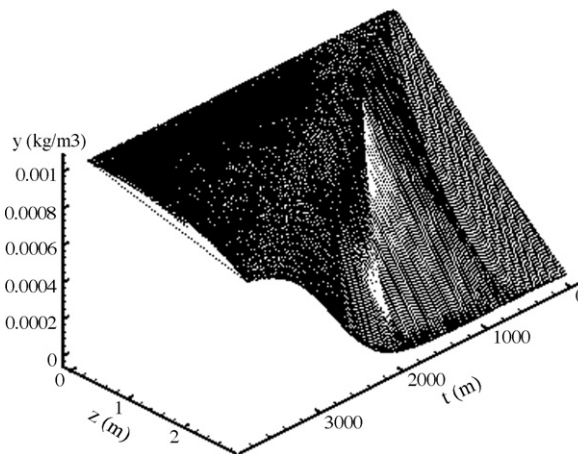


Fig. 13. Concentration distribution of H<sub>2</sub>S in the middle of reactor in axial at different time by model calculation.

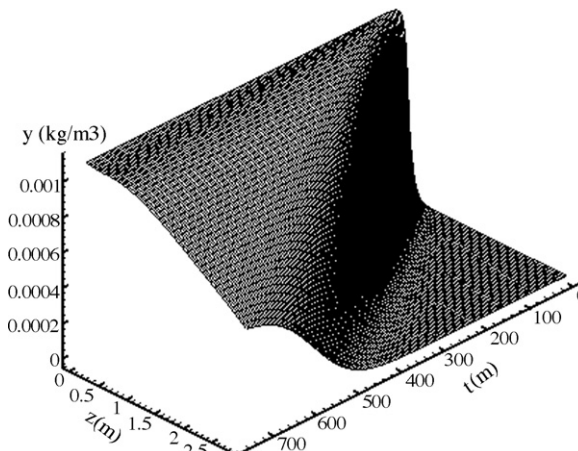


Fig. 14. Concentration distribution of PH<sub>3</sub> in the middle of reactor in axial at different time by model calculation.



## 6. Conclusion

Two kinds of impregnated activated carbon were prepared to remove H<sub>2</sub>S and PH<sub>3</sub> in yellow phosphorous tail gas. The removal of H<sub>2</sub>S and PH<sub>3</sub> through a impregnated activated carbon fixed bed can be considered as an adsorptive reaction process which involves two independent processes: physical adsorption and catalytic oxidation reaction. The performances of laboratory-scale and pilot-plant fixed bed have been assessed for both impregnated activated carbon. A mixture catalyze was used to remove both S and P compounds simultaneously in real yellow phosphorous tail gas. Adsorption kinetic and reaction kinetic of this process were studied over the mixture impregnated activated carbon. After purification through the catalyze bed, the concentration of H<sub>2</sub>S and PH<sub>3</sub> in tail gas would be PH<sub>3</sub> < 5 mg/m<sup>3</sup>, H<sub>2</sub>S < 5 mg/m<sup>3</sup>, which can be used as a source for further products.

A two-dimensional non-steady binary mixture gases adsorption-reaction mathematical model were developed to simulated the pilot-plant reactor for removing H<sub>2</sub>S and PH<sub>3</sub> simultaneously. On the whole, the model predictions match the experimental pilot-plant data for both compounds. From the prediction of model, the detail concentration distribution of compounds in gas or solid phase can be observed. It is thus a very useful tool to support the proper design of industrial yellow phosphorous tail gas purification unit.

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